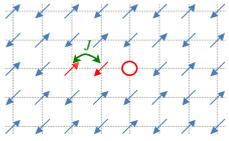


# Exciton condensation in strongly correlated electron bilayers

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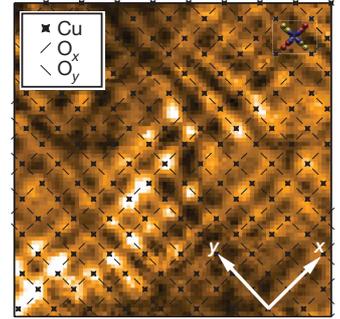
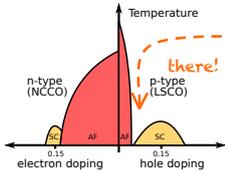
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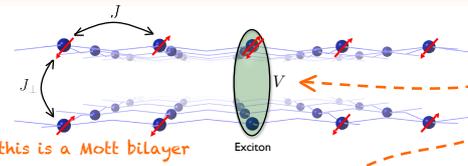
Mott insulator with a single hole

## Why strongly correlated materials?

- The parent-compounds of the high-temperature superconducting cuprates are layered Mott insulators: one localized electron spin on each lattice site.
- Upon doping, a whole zoo of complex ordered phases appear in between the antiferromagnetic phase and the superconducting phase.
- There exists no good theory due to strong electron interactions. The fermionic nature of electrons makes it impossible to solve Hamiltonians or to use Monte-Carlo.



Eun-Ah Kim and co-workers showed this complex electronic patterns in BSCCO [1]



this is a Mott bilayer

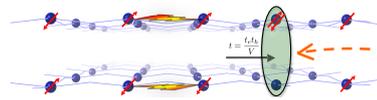
## New: bilayer excitons

A bilayer exciton is the bound state of a doubly occupied and a vacant site.

We have shown that the dynamics of a single (bosonic) exciton shows frustration effects similar to the (fermionic) hole in a single layer. [2]  
Hence now we can try to understand complex ordered phases in a purely bosonic theory!

## Basic theoretical parameters

- Magnetic exchange coupling, both in-plane  $J$  and inter-plane  $J_{\perp}$
- Hopping of exciton  $t$  scrambles up AF order



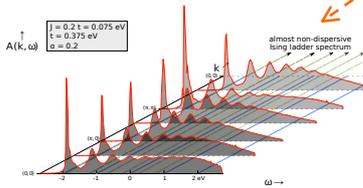
AF order is scrambled!

## Model Hamiltonian

$$\mathcal{H} = J \sum_{\langle ij \rangle} \mathbf{S}_{i1} \cdot \mathbf{S}_{j1} + J_{\perp} \sum_i \mathbf{S}_{i1} \cdot \mathbf{S}_{i2} - t \sum_{\langle ij \rangle} |E_j\rangle \left( |0 0\rangle_i \langle 0 0|_j + \sum_m |1 m\rangle_i \langle 1 m|_j \right) \langle E_i|$$

Heisenberg terms

Hopping term = exchange of exciton  $|E\rangle$  with magnetic states  $|s m\rangle$



The spectral function of a bilayer exciton

## Mean field phase diagram

### EC = Exciton condensate

Superposition on each site of singlet ground state with exciton:

$$\prod_i (u_i + v_i \hat{E}_i^{\dagger}) |0 0\rangle$$

Usually, an exciton condensate is detectable via its enhanced interlayer tunneling. [3]  
However, because of the singlet ground state the tunneling of opposite spin species cancels each other. Consequently, the 'singlet exciton condensate' has no tunneling matrix element and is therefore a 'dark' exciton condensate.

### EI = Excitonic insulator

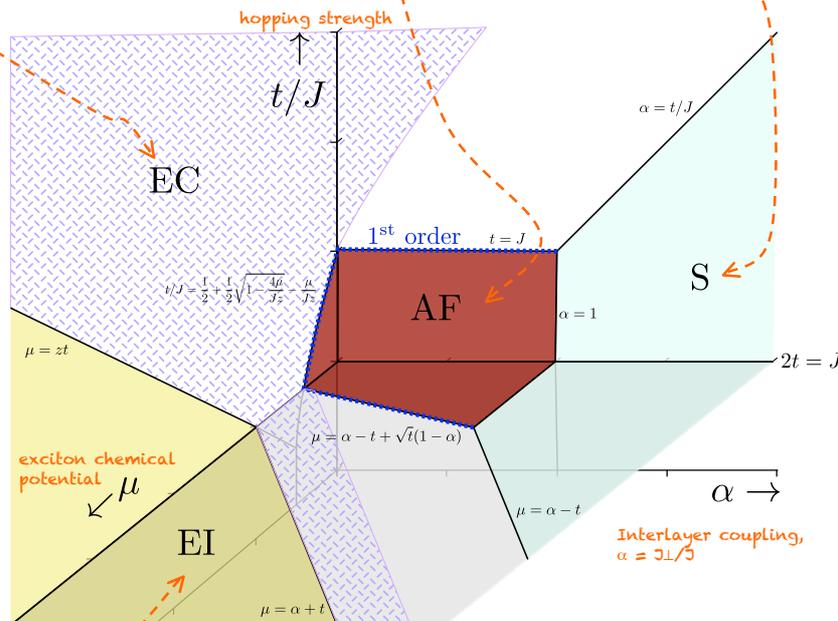
Boring phase with only excitons.

### AF = Antiferromagnetism

Just the normal Néel state, without excitons.

### S = Rung singlets

Boring phase without excitons, on each interlayer rung there is a singlet of electron spins.



## Inhomogeneous phases

In the shaded region, the mean field solution is instable towards inhomogeneities.

Amongst the possibilities:

- Stripe phases can appear: one-dimensional ordering of exciton density.
- Phase separation of excitonic regions and magnetically ordered regions.
- Domain walls or other topological structures in the magnetic order can couple to exciton condensate vortices.

The role of electric dipole exciton-exciton interaction in phase formation is still a subtle question.

## References

- [1] Mesáros, et al. Science **333**, 426 (2011)
- [2] Rademaker, Wu, Hilgenkamp and Zaanen, EPL **97** 27004 (2012)
- [3] Eisenstein and MacDonald, Nature **432**, 691 (2004)

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